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Education

KwaZulu-Natal Department of Education

MATHEMATICS P2

MARKING GUIDELINE

PREPARATORY EXAMINATION

SEPTEMBER 2018

**NATIONAL
SENIOR CERTIFICATE**

GRADE 12

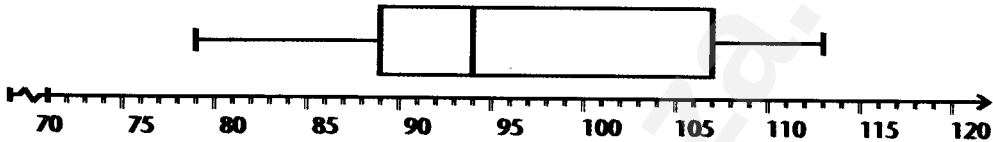
MARKS: 150

This marking guideline consists of 14 pages.

QUESTION 1

1.1	strong positive trend	✓ A strong positive	(1)
1.2	(38; 127)	✓ A answer	(1)
1.3	$a = 68,66$ $b = 2,46$ $y = 68,66x + 2,46x$	✓ A $a = 68,66$ ✓ A $b = 2,46$ ✓ CA equation	(3)
1.4	$y = 68,66 + 2,46 (24)$ $= 127,7$ $= 127$	✓ CA ✓ CA answer	(2)
			[7]

QUESTION 2

2.1	$\text{Mean weight} = \bar{x} = \frac{1443}{15}$ $= 96,2 \text{ kg}$	✓ A sum divided by 15 ✓ CA answer (only if dividing by 15)	(2)
2.2	$\sigma = \text{standard deviation} = 11,27$	✓✓ AA answer	(2)
2.3	$(\bar{x} - \sigma; \bar{x} + \sigma)$ $= (84,93; 107,47)$ Therefore 2 scores are less than the standard deviation	✓ CA identify range ✓ CA answer	(2)
2.4		✓ A min value 79 ✓ A $Q_1 = 89$ ✓ A $Q_2 = 94$ ✓ A $Q_3 = 107$ ✓ A max value = 113	(5)
2.5	$\text{IQR} = Q_3 - Q_1$ $= 107 - 89$ $= 18$	✓ CA difference ✓ CA answer	(2)
2.6	$\bar{x} - \text{median} = 96,2 - 94,00$ $= 2,2$ Data is positively skewed.	✓ CA answer	(1)
			[14]

QUESTION 3

3.1.1	$m_{AB} = \frac{y_2 - y_1}{x_2 - x_1}$ $= \frac{1 - 5}{4 - (-4)}$ $= \frac{-4}{8}$ $= \frac{-1}{2}$	✓ A substitution into gradient formula ✓ CA answer (provided – answer)	(2)
3.1.2	$y = mx + c$ $5 = -\frac{1}{2}(-4) + c$ $c = 3$ $y = -\frac{1}{2}x + 3$	✓ CA substituting point and gradient of line AB ✓ CA answer	(2)
3.1.3	$m_{CD} = 2 \quad CD \perp AB$ $y = mx + c$ $-4 = 2(-1) + c$ $c = -2$ $y = 2x - 2$	✓ CA $CD \perp AB$ ✓ A substituting point (-1;-4) ✓ CA answer	(3)
3.1.4	$\therefore 2x - 2 = -\frac{1}{2}x + 3$ $\frac{5}{2}x = 5$ $\therefore x = 2$ $\therefore y = 2(2) - 2$ $= 2$ $\therefore E(2; 2)$	✓ CA Equating ✓ CA $x = 2$ ✓ CA $y = 2$ (CA if both co-ordinates are positive)	(3)

$$\begin{aligned} & \sqrt{(2 - (-1))^2 + (2 - (-4))^2} \\ &= \sqrt{9 + 36} \\ &= \sqrt{45} \\ &= 3\sqrt{5} \end{aligned}$$

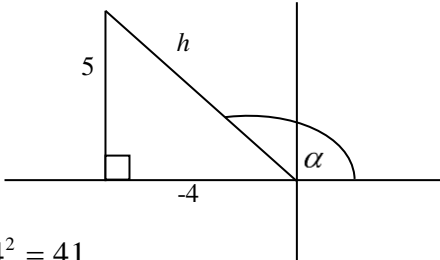
$$\begin{aligned} & \sqrt{(2 - (-4))^2 + (2 - 5)^2} \\ &= \sqrt{36 + 9} \\ &= \sqrt{45} \\ &= 3\sqrt{5} \end{aligned}$$

$$\begin{aligned} \text{of } \triangle AEC &= \frac{1}{2} \text{ base} \times \text{height} \\ &= \frac{1}{2} \cdot 3\sqrt{5} \times 3\sqrt{5} \\ &= \frac{1}{2} \cdot 9 \times 5 \\ &= \frac{45}{2} \\ &= 22,5 \text{ units}^2 \end{aligned}$$

QUESTION 4

4.1	P(6 ; - 2)	✓ A x – value ✓ A y - value	(2)
4.2	$2x - 4 = 0$ $x = 2$ S(2 ; 0)	✓ A equating to 0 ✓ A x – value	(2)
4.3	$\hat{ABC} = 90^\circ$ Angle in a semi-circle $m_{BC} = -\frac{1}{2}$ AB $\perp$ BC $y = mx + c$ $2 = -\frac{1}{2}(3) + c$ $c = \frac{7}{2}$ $y = -\frac{1}{2}x + \frac{7}{2}$	✓ A Statement ✓ A gradient of BC ✓ A substitution of point (3 ; 2) ✓ CA answer	(4)
4.4	R(7 ; 0) x int of BC $BR^2 = (7 - 3)^2 + (0 - 2)^2 = 20$ $(x - 7)^2 + (y - 0)^2 = 20$	✓ CA for 7 ✓ A for 0 coordinates of R ✓ CA subst. into distance formula ✓ CA radius value ✓ CA answer	(5)
4.5	$m_{PS} = -\frac{1}{2}$ $\therefore PS \parallel CB$ equal gradients A(1; - 2) midpoint formula Since the y – coordinates of A and P is – 2 Therefore AC//SR OR $m_{AC} = 0$... (both y values are the same) $m_{SR} = 0$... (x–axis) $\therefore m_{AC} = m_{SR}$ $\therefore AC \parallel SR$	✓ A ✓ A gradient of PS ✓ A PS//CB ✓ A coordinates of A ✓ A Reasoning ✓ A Statement ✓ A Reason ✓ A Statement ✓ A Reason ✓ A $m_{AC} = m_{SR}$	(5) [18]

QUESTION 5

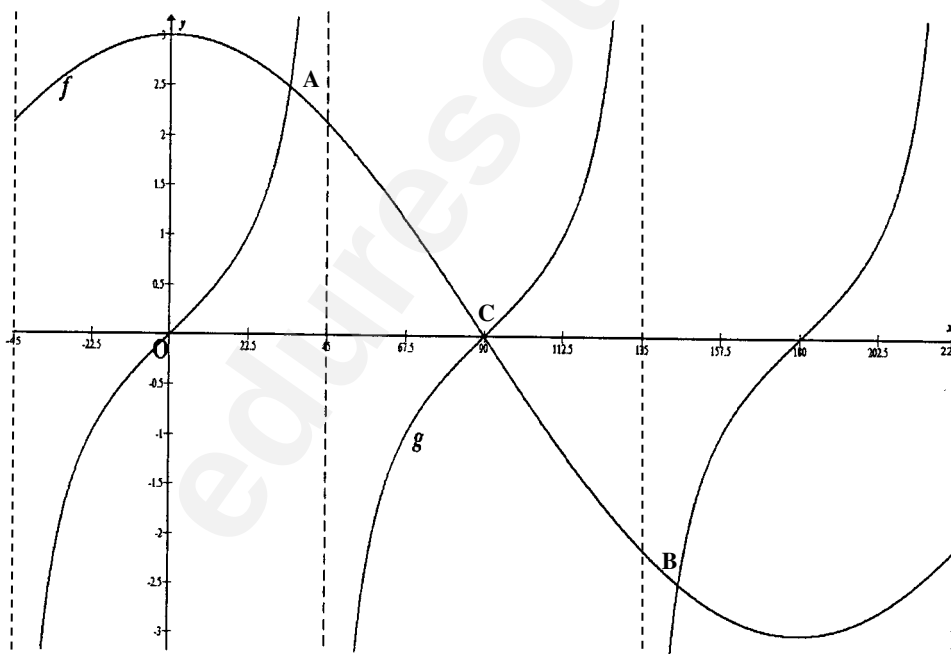
5.1	$4 \tan \alpha + 5 = 0$ $\tan \alpha = \frac{-5}{4}$  $h^2 = 5^2 + 4^2 = 41$ $\therefore h = \sqrt{41}$ $\cos 180^\circ = -1$ $\sin(-150^\circ) = -\sin 30^\circ$ $= -\frac{1}{2}$ $\sqrt{41} \left(\frac{-4}{\sqrt{41}} \right) - 4 \left(-\frac{1}{2} \right) (-1) = -4 - 2 = -6$	✓ A diagram in the correct quadrant ✓ A $\sqrt{41}$ ✓ A -1 ✓ A $-\frac{1}{2}$ ✓ CA answer	(5)
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5.2.1	$\frac{\cos 99^\circ - \sin 99^\circ}{\cos 33^\circ \sin 33^\circ}$ $= \frac{\cos 99^\circ \sin 33^\circ - \sin 99^\circ \cos 33^\circ}{\cos 33^\circ \sin 33^\circ}$ $= \frac{-[\sin 99^\circ \cos 33^\circ - \cos 99^\circ \sin 33^\circ]}{\cos 33^\circ \sin 33^\circ}$ $= \frac{-\sin(99^\circ - 33^\circ)}{\cos 33^\circ \sin 33^\circ}$ $= \frac{-\sin 66^\circ}{\cos 33^\circ \sin 33^\circ}$ $= \frac{-2 \sin 33^\circ \cos 33^\circ}{\cos 33^\circ \sin 33^\circ}$ $= -2$	✓ A Simplification ✓ A Taking negative sign out ✓ A $\sin(99^\circ - 33^\circ)$ ✓ A $\sin 66^\circ$ ✓ A $2 \sin 33^\circ \cos 33^\circ$ ✓ A answer	(6)
5.2.2	$= \frac{-\cos 40^\circ - (\cos \theta)}{\sin 50^\circ + \cos \theta}$ $= \frac{-\cos 40^\circ - (\cos \theta)}{\cos 40^\circ + \cos \theta} = \frac{-(\cos 40^\circ + \cos \theta)}{(\cos 40^\circ + \cos \theta)}$ $= -1$	✓ A $-\cos 40^\circ$ ✓ A $\cos \theta$ (numerator) ✓ A $\sin 50^\circ$ ✓ $\cos \theta$ (denominator) ✓ CA answer	(5)
5.3	$\frac{2 \sin^2 x}{2 \tan x - \sin 2x} = \frac{\cos x}{\sin x}$ <i>LHS</i> $= \frac{2 \sin^2 x}{\frac{2 \sin x}{\cos x} - 2 \sin x \cos x}$ $= \frac{2 \sin^2 x}{\frac{2 \sin x - 2 \sin x \cos^2 x}{\cos x}}$ $= \frac{2 \sin^2 x \cdot \cos x}{2 \sin x - 2 \sin x \cos^2 x}$ $= \frac{2 \sin^2 x \cos x}{2 \sin x [1 - \cos^2 x]}$ $= \frac{2 \sin x \cos x}{\sin^2 x}$ $= \frac{\cos x}{\sin x}$ $= RHS$	✓ A $2 \sin x \cos x$ ✓ A $\frac{\sin x}{\cos x}$ ✓ A Simplification ✓ A removal of common factor of $2 \sin x$ ✓ A $\frac{\sin x \cos x}{\sin^2 x}$	(5)

5.4	$8 \sin \theta \cos \theta = -2\sqrt{3}$ $\frac{8 \sin \theta \cos \theta}{4} = \frac{-2\sqrt{3}}{4}$ $2 \sin \theta \cos \theta = \frac{-\sqrt{3}}{2}$ $\sin 2\theta = \frac{-\sqrt{3}}{2}$ reference angle = 60° $2\theta = (180^\circ + 60^\circ) + k \cdot 360^\circ, k \in \mathbb{Z}$ $2\theta = 240^\circ + k \cdot 360^\circ, k \in \mathbb{Z}$ $\theta = 120^\circ + k \cdot 180^\circ, k \in \mathbb{Z}$ OR $2\theta = (360^\circ - 60^\circ) + k \cdot 360^\circ, k \in \mathbb{Z}$ $2\theta = 300^\circ + k \cdot 360^\circ, k \in \mathbb{Z}$ $\theta = 150^\circ + k \cdot 180^\circ, k \in \mathbb{Z}$	✓ A dividing by 4 both sides ✓ A $2 \sin \theta \cos \theta = \sin 2\theta$ ✓ A 60° ✓ CA 240° ✓ CA $\theta = 120^\circ + k \cdot 180^\circ, k \in \mathbb{Z}$ ✓ CA 300° ✓ CA $\theta = 150^\circ + k \cdot 180^\circ, k \in \mathbb{Z}$	(7)
			[29]

QUESTION 6

6.1



- ✓ A shape of f
- ✓ A shape of g
- ✓ A A asymptotes
- ✓ A x -intercepts of f
- ✓ A Turning points of f
- ✓ A x -intercepts of g
- ✓ A 3 intersection points

(8)

6.2	the graphs intersect at A, B and C. At A we have $x = 34^\circ$, at C we have $x = 90^\circ$ and by using symmetry we get at B, $x = 180^\circ - 34^\circ = 146^\circ$.	✓ A using symmetry ✓ A answer Answer only full marks	(2) [10]
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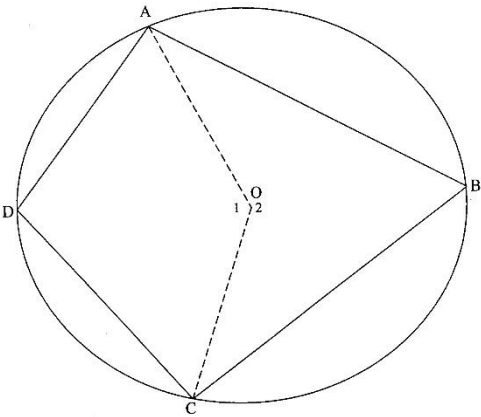
$\frac{2y}{\sin 2y}$ $\frac{PQ}{\sin 2y}$ $\frac{y}{\sin 2y}$ $\frac{\cos y}{\sin 2y}$	$\checkmark PQ = \frac{h \cos y}{\sin y}$ $\checkmark \hat{PQR} = 90^\circ - y$ $\checkmark \text{applying sine rule}$ $\checkmark \sin (90^\circ - y) = \frac{PQ}{h}$ $\checkmark \text{subst PQ} = \frac{h \cos y}{\sin y}$
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from centre $\perp$ ch

from centre $\perp$ ch

=	$\frac{36,7}{2}$ cm	✓CA answer
=	18,4 cm	

QUESTION 9

9.1	 Construction: Draw AO and CO <u>Proof:</u> $\hat{O}_1 = 2\hat{B} \dots \angle \text{ at centre} = 2 \angle \text{ at circle}$ $\hat{O}_2 = 2\hat{D} \dots \angle \text{ at centre} = 2 \angle \text{ at circle}$ $\hat{O}_1 + \hat{O}_2 = 360^\circ$ $2\hat{B} + 2\hat{D} = 360^\circ$ $\hat{B} + \hat{D} = 180^\circ$	✓ A Construction ✓ A S/R ✓ A S/R ✓ A $\hat{O}_1 + \hat{O}_2 = 360^\circ$ (revolution) ✓ A Substitute for $\hat{O}_1$ and $\hat{O}_2$	(5)
9.2.1	$\hat{K}_1 = x = \hat{K}_2 \dots$ KM bisects $\hat{L}\hat{K}\hat{N}$ $\hat{O}_1 = 2x$ angles opp = sides $\therefore \hat{L} = x$ $\angle \text{ at centre} = 2 \angle \text{ at circumference}$ $\therefore \hat{K}_1 = \hat{L} = x$ $\therefore \text{TK} = \text{TL}$ (sides opposite equal angles)	(All Accuracy Marks) ✓ S ✓ R ✓ S ✓ R ✓ R	(5)

9.2.2	$\hat{T}_1 = 2x \dots \text{ext } \angle \text{ of } \Delta QKL$ $\hat{T}_1 = \hat{O}_1 = 2x$ $\therefore$ KOTP is a cyclic quadrilateral ... converse of $\angle$'s on the same segment equal.	$\checkmark$ S $\checkmark$ R $\checkmark$ R (All Accuracy Marks)	(3)
9.2.3	$\hat{P}_1 = \hat{LKN} \dots$ Angles in the same segment $= 2x$ $\therefore \hat{P}_1 = \hat{T} = 2x$ $\therefore PN \parallel MK \dots$ alt $\angle$'s proved equal	$\checkmark$ S $\checkmark$ R $\checkmark$ R (All Accuracy Marks)	(3)
			[16]

QUESTION 10

10.1	$\frac{AS}{SP} = \frac{AR}{RB} \dots RS \parallel BP$ $= \frac{3}{2}$ $\therefore \frac{AS}{SC} = \frac{3}{7}$	$\checkmark$ S/R $\checkmark \frac{3}{2}$ $\checkmark \frac{3}{7}$ (All Accuracy Marks)	(3)
10.2	$\frac{RT}{TC} = \frac{SP}{PC} \dots RS \parallel TP$ $= \frac{2}{5}$	$\checkmark$ S/R $\checkmark \frac{2}{5}$	(2)
10.3	$\frac{\Delta ARS}{\Delta ABC} = \frac{\Delta ARS}{\Delta ARC} \times \frac{\Delta ARC}{\Delta ABC}$ $= \frac{3}{10} \times \frac{3}{5}$ $= \frac{9}{50}$	$\checkmark$ ratio of Δ 's $\checkmark$ substitution $\checkmark$ CA answer (All Accuracy Marks if not indicated)	(3)
			[8]

QUESTION 11

11.1 In $\triangle PAT$ and $\triangle PCA$ 1. $\hat{P}$ is common 2. $\hat{A}_1 = \hat{C}_1$ tan chord thrm. 3 $P\hat{T}A = P\hat{A}C$ sum of angles in triangle $\therefore \triangle PAT \parallel \triangle PCA$ ($\angle\angle\angle$) $\therefore \frac{PA}{PC} = \frac{PT}{PA}$ ($\parallel \triangle$'s) $\therefore PA^2 = PC \cdot PT$	✓ S (identifying triangles) ✓ S ✓ S ✓ S/R ✓ S All accuracy marks	(5)
11.2 $PA^2 = PC \cdot PT$ $\therefore 36 = (x + 5) x$ $\therefore 36 = x^2 + 5x$ $\therefore x^2 + 5x - 36 = 0$	✓ A subst. ✓ A simplifying	(2)
11.3 $(x + 9)(x - 4) = 0$ $x = -9$ or $x = 4$ N/A $\therefore PT = 4$ units	✓ A factorising ✓ A $PT = 4$	(2)
11.4 $\frac{PD}{PA} = \frac{PT}{PC}$ (AC//DB; prop. theorem) $DP = \frac{4}{9} \cdot 6$ $= \frac{8}{3}$	✓S ✓R ✓CA answer	(3)
[12]		

TOTAL MARKS: 150