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**NATIONAL  
SENIOR CERTIFICATE**

**GRADE/GRADE 12**

**SEPTEMBER 2016**

**MATHEMATICS P2 / *WISKUNDE V2*  
MEMORANDUM**

**MARKS / PUNTE: 150**

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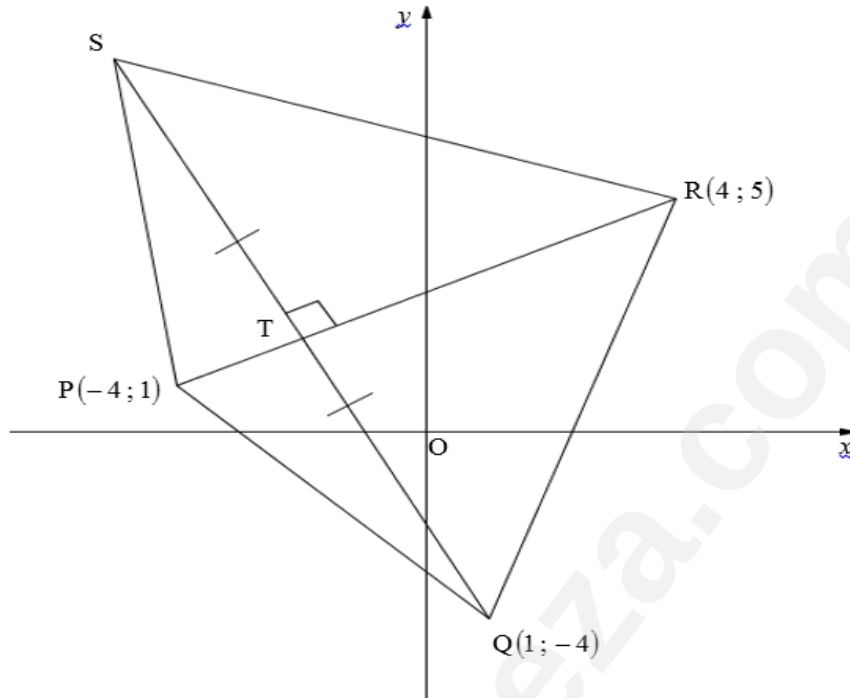
This memorandum consists of 16 pages.  
*Hierdie memorandum bestaan uit 16 bladsye.*

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| QUESTION 1 / VRAAG 1 |                                                                                                                                                                                                                                             |     |     |     |    |                                                                                                                                                                                |                                                                                                                                                                                                                               |    |     |      |
|----------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----|-----|-----|----|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----|-----|------|
|                      | Day/Dag                                                                                                                                                                                                                                     | 0   | 1   | 4   | 6  | 9                                                                                                                                                                              | 12                                                                                                                                                                                                                            | 17 | 19  |      |
|                      | Weight / Gewig                                                                                                                                                                                                                              | 124 | 121 | 103 | 90 | 71                                                                                                                                                                             | 50                                                                                                                                                                                                                            | 27 | 16  |      |
| 1.1                  |                                                                                                                                                                                                                                             |     |     |     |    |                                                                                                                                                                                | <ul style="list-style-type: none"><li>✓ 2-4 correct points</li><li>✓ 5-7 correct points</li><li>✓ plotting all points</li><br/><li>✓ 2 – 4 punte korrek</li><li>✓ 5 – 7 punte korrek</li><li>✓ alle punte afgesteek</li></ul> |    |     | (3)  |
| 1.2                  | $a = 124,84$<br>$b = -5,83$<br>$y = 124,84 - 5,83x$                                                                                                                                                                                         |     |     |     |    | <ul style="list-style-type: none"><li>✓ A</li><li>✓ B</li><li>✓ equation / vergelyking</li></ul>                                                                               |                                                                                                                                                                                                                               |    | (3) |      |
| 1.3                  | $(x; y) = (8; 5; 75,25)$<br>$y$ -int 124,84                                                                                                                                                                                                 |     |     |     |    | <ul style="list-style-type: none"><li>✓ <math>(8; 5; 75,25)</math> and/en <math>y</math>-int / <math>y</math>-afsnit 124,84</li><li>✓ regression line / regressielyn</li></ul> |                                                                                                                                                                                                                               |    | (2) |      |
| 1.4                  | $124,84 - 5,83x = 80$<br>$5,83x = 44,84, 69$<br>$x = 7,69$<br>On the morning of the 8 <sup>th</sup> day the bar of soap will be less than 80 grams. <i>Op die oggend van die 8<sup>ste</sup> dag sal steen seep minder as 80 gram wees.</i> |     |     |     |    | <ul style="list-style-type: none"><li>✓ substitution / vervanging</li><li>✓ answer / antwoord</li></ul>                                                                        |                                                                                                                                                                                                                               |    | (2) |      |
| 1.5                  | $r = -0,998$                                                                                                                                                                                                                                |     |     |     |    |                                                                                                                                                                                | <ul style="list-style-type: none"><li>✓ answer / antwoord</li></ul>                                                                                                                                                           |    |     | (1)  |
| 1.6                  | Very strong negative correlation. <i>Baie sterk negatiewe korrelasie.</i>                                                                                                                                                                   |     |     |     |    |                                                                                                                                                                                | <ul style="list-style-type: none"><li>✓ answer / antwoord</li></ul>                                                                                                                                                           |    |     | (1)  |
|                      |                                                                                                                                                                                                                                             |     |     |     |    |                                                                                                                                                                                |                                                                                                                                                                                                                               |    |     | [12] |

| QUESTION 2 / VRAAG 2 |                                                                                                                                                                                                                                  |                                                                                    |            |
|----------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------|------------|
| 5                    | 7                                                                                                                                                                                                                                |                                                                                    |            |
| 4                    | 3 4 4                                                                                                                                                                                                                            |                                                                                    |            |
| 3                    | 1 1 1 4 6 8                                                                                                                                                                                                                      |                                                                                    |            |
| 2                    | 2 4 8 9 9                                                                                                                                                                                                                        |                                                                                    |            |
| 1                    | 5 5 6 7                                                                                                                                                                                                                          |                                                                                    |            |
| 0                    | 3 5                                                                                                                                                                                                                              |                                                                                    |            |
| 2.1                  | 21 learners / <i>leerders</i>                                                                                                                                                                                                    | ✓ answer / <i>antwoord</i>                                                         | (1)        |
| 2.2                  | 3 pages / <i>bladsye</i>                                                                                                                                                                                                         | ✓ answer / <i>antwoord</i>                                                         | (1)        |
| 2.3                  | $\bar{x} = 28,19$                                                                                                                                                                                                                | ✓✓ answer / <i>antwoord</i>                                                        | (2)        |
| 2.4                  | $\sigma = 13,12$                                                                                                                                                                                                                 | ✓ answer / <i>antwoord</i>                                                         | (1)        |
| 2.5                  | $(28,19 - 13,12; 28,19 + 13,12)$<br>$(15,07; 41,31)$<br><br>$\therefore$ 8 learners are outside one standard deviation<br><i>8 leerders is buite een standaardafwyking</i><br><br>$\therefore \frac{8}{21} \times 100 = 38,10\%$ | ✓ interval / <i>interval</i><br><br>✓ 8 learners / <i>leerders</i><br><br>✓ 28,57% | (3)        |
|                      |                                                                                                                                                                                                                                  |                                                                                    | <b>[8]</b> |

## QUESTION 3 / VRAAG 3

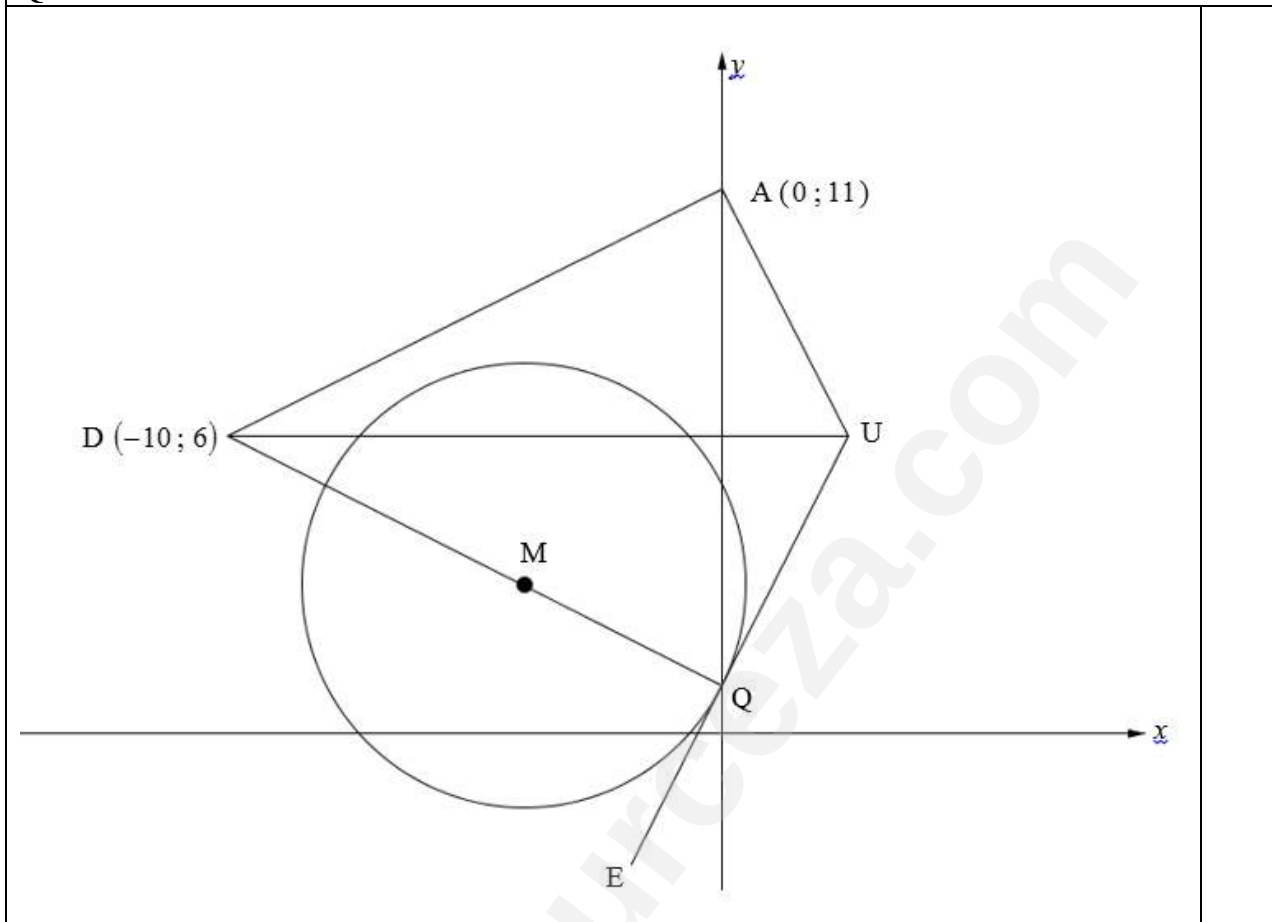


|     |                                                                                                                                                                                                                                                   |                                                                                                                                                                                                                                                                                                                                  |     |
|-----|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----|
| 3.1 | $m_{PR} = \frac{5-1}{4+4}$ $= \frac{1}{2}$                                                                                                                                                                                                        | <ul style="list-style-type: none"> <li>✓ subst. P and R into correct formula<br/>verv. van P en R in korrekte formule</li> <li>✓ <math>m_{PR} = \frac{1}{2}</math></li> </ul>                                                                                                                                                    | (2) |
| 3.2 | $m_{SQ} = -2$ $SP \perp PT$<br>$y + 4 = -2(x - 1)$<br>$y = -2x - 2$                                                                                                                                                                               | <ul style="list-style-type: none"> <li>✓ <math>m_{SQ} = -2</math></li> <li>✓ subst. m and Q into correct formula<br/>verv. van m en Q in korrekte formule</li> <li>✓ <math>y = -2x - 2</math></li> </ul>                                                                                                                         | (3) |
| 3.3 | <p>Equation of PR / Vergelyking van PR</p> $y - 1 = \frac{1}{2}(x + 4)$ $y = \frac{1}{2}x + 3$ $-2x - 2 = \frac{1}{2}x + 3$ $-4x - 4 = x + 6$ $-5x = 10$ $\therefore x = -2$ $y = -2(-2) - 2 = 2$ <p style="text-align: center;"><b>OR/OF</b></p> | <ul style="list-style-type: none"> <li>✓ substituting m and P into equation of a str. line / vervanging van m en P in die vergelyking van reguitlyn</li> <li>✓ equation of PR / vergelyking van PR</li> <li>✓ equating PR and SQ / gelykstel van PR en SQ</li> <li>✓ x-value / x-waarde</li> <li>✓ y-value / y-waarde</li> </ul> |     |

✓ substituting m and R into equation of a

|     |                                                                                                                                                                                                                                                                                                                                                                                              |                                                                                                                                                                                                                                                                                                                                                                                    |             |
|-----|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------|
|     | $y - 5 = \frac{1}{2}(x - 4)$ $2y - 10 = x - 4$ $2y = x + 6$ $y = \frac{1}{2}x + 3$ $-2x - 2 = \frac{1}{2}x + 3$ $-4x - 4 = x + 6$ $-5x = 10$ $\therefore x = -2$ $y = -2(-2) - 2 = 2$                                                                                                                                                                                                        | str. line / <i>vervanging van m en R in die vergelyking van reguitlyn</i><br>✓ equation of PR / <i>vergelyking van PR</i><br>✓ equating PR and SQ / <i>gelykstel van PR en SQ</i><br>✓ x-value / <i>x-waarde</i><br>✓ y-value / <i>y-waarde</i>                                                                                                                                    | (5)         |
| 3.4 | $-2 = \frac{x+1}{2} \quad 2 = \frac{y-4}{2}$ $\therefore x = -5 \quad \text{and/en} \quad y = 8$ $S(-5; 8)$                                                                                                                                                                                                                                                                                  | ✓ substituting into correct formula / <i>vervanging in korrekte formule</i><br>✓ x-value / <i>x-waarde</i><br>✓ y-value / <i>y-waarde</i>                                                                                                                                                                                                                                          | (3)         |
| 3.5 | $SQ = \sqrt{(-5-1)^2 + (8+4)^2}$ $= 6\sqrt{5}$ $PT = \sqrt{(-2+4)^2 + (2-1)^2}$ $= \sqrt{5}$ $\text{Area } \Delta PQS = \frac{1}{2} \times 6\sqrt{5} \times \sqrt{5}$ $= 15 \text{ unit}^2 / \text{eenhede}^2$ <p style="text-align: center;"><b>OR/OF</b></p> $\therefore \text{area of } \Delta PQS = ST \times PT$ $= 3\sqrt{5} \times \sqrt{5}$ $= 15 \text{ unit}^2 / \text{eenhede}^2$ | ✓ subst. into correct form / <i>verv. in korrekte formule</i><br>✓ $SQ = 6\sqrt{5}$<br>✓ $PT = \sqrt{5}$<br>✓ Subt into correct form. / <i>verv. in korrekte formule</i><br>✓ $15 \text{ units}^2 / \text{eenhede}^2$<br>✓ $SQ = 6\sqrt{5}$<br>✓ $ST = 3\sqrt{5}$<br>✓ $PT = \sqrt{5}$<br>✓ subst into form / <i>verv. in formule</i><br>✓ $15 \text{ units}^2 / \text{eenhede}^2$ | (5)         |
|     |                                                                                                                                                                                                                                                                                                                                                                                              |                                                                                                                                                                                                                                                                                                                                                                                    | <b>[18]</b> |

## QUESTION 4 / VRAAG 4



|     |                                                                                                                                                                                                          |                                                                                                                                                                                                                                                                                                                                                                                      |     |
|-----|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----|
| 4.1 | $x^2 + 8x + 16 + y^2 - 6y + 9 = 20$ $(x + 4)^2 + (y - 3)^2 = 20$ $\therefore M(-4; 3)$                                                                                                                   | <ul style="list-style-type: none"> <li>✓ completing square<br/><i>kwadraatsvoltooing</i></li> <li>✓ <math>(x + 4)^2 + (y - 3)^2 = 20</math></li> <li>✓ x-coordinate / x-koördinaat</li> <li>✓ y-coordinate / y-koördinaat</li> </ul>                                                                                                                                                 | (4) |
| 4.2 | $(0 + 4)^2 + (y - 3)^2 = 20$ $(y - 3)^2 = 4$ $y = 3 \pm 2$ $\therefore y = 1$ $Q(0; 1)$                                                                                                                  | <ul style="list-style-type: none"> <li>✓ subst. <math>x = 0</math> into circle equation<br/><i>verv. <math>x = 0</math> in sirkel vergelyking</i></li> <li>✓ <math>(y - 3)^2 = 4</math></li> <li>✓ <math>y = 1</math></li> </ul>                                                                                                                                                     | (3) |
| 4.3 | $m_{\text{radius}} = \frac{3 - 1}{-4 - 0} = -\frac{1}{2}$ $m_{\text{tan/rkl}} = 2$ $y - 1 = 2(x - 0) \quad [\text{tangent } \perp \text{ radius}]$ $\therefore y = 2x + 1 \quad [\text{raaklyn } \perp]$ | <ul style="list-style-type: none"> <li>✓ <math>m_{\text{rad}} = -\frac{1}{2}</math></li> <li>✓ <math>m_{\text{tan}} = 2</math> / <math>m_{\text{raaklyn}} = 2</math></li> <li>✓ subst. <math>m_{\text{tan/rkl}} = 2</math> and Q into correct form. / <i>verv. <math>m_{\text{tan/rkl}} = 2</math> en Q in korrekte formule.</i></li> <li>✓ equation / <i>vergelyking</i></li> </ul> | (4) |
| 4.4 | $y = 6$                                                                                                                                                                                                  | ✓ answer / <i>antwoord</i>                                                                                                                                                                                                                                                                                                                                                           | (1) |

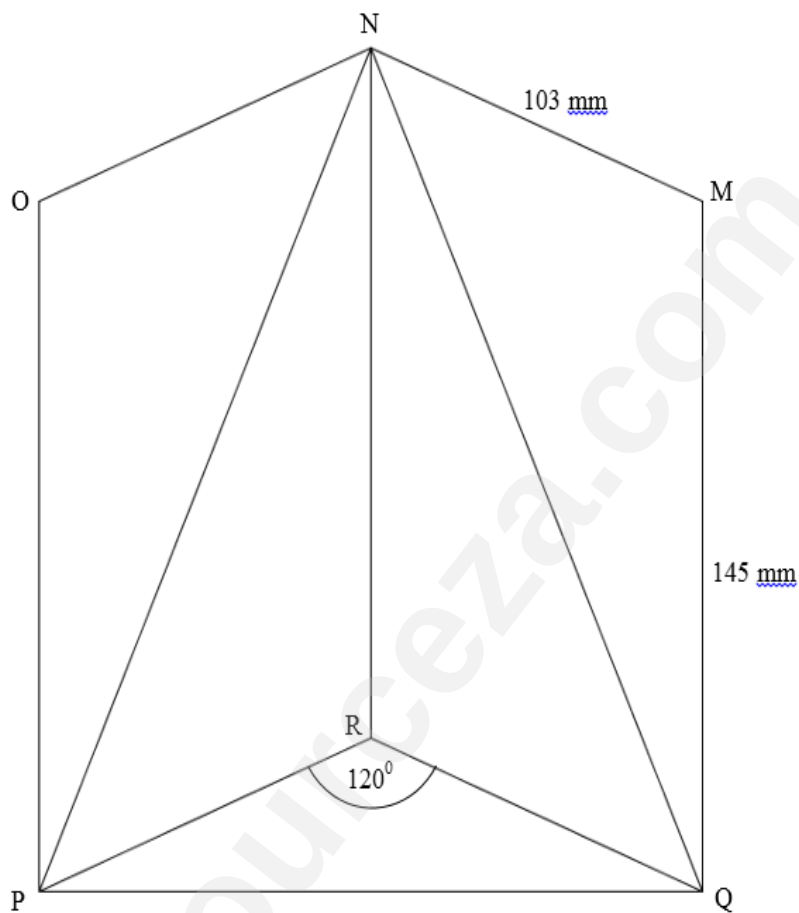
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|-----|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------|
| 4.5 | $6 = 2x + 1$<br>$x = \frac{5}{2}$<br>$U\left(\frac{5}{2}; 6\right)$                                                                                                                                                                                                                                                                                                                                                                                                                                  | $\checkmark \quad 6 = 2x + 1$<br>$\checkmark \quad x = \frac{5}{2}$                                                                                                                                                                   | (2)  |
| 4.6 | $m_{AU} = \frac{11-6}{0-\frac{5}{2}}$<br>$= -2$<br>$m_{AD} = \frac{6-11}{-10-0}$<br>$= \frac{1}{2}$<br>$m_{AU} \times m_{DA} = -2 \times \frac{1}{2}$<br>$= -1$<br>$\therefore AU \perp DA$<br>$\therefore \hat{A} = 90^\circ$<br>$D\hat{Q}U = 90^\circ$ [tangent $\perp$ radius] / [raaklyn $\perp$ radius]<br>$\therefore$ QUAD is a cyclic quad. [opp. $\angle^s$ add up to $180^\circ$ ]<br><i>QUAD is 'n koordevierhoek [teenoorst. <math>\angle^e</math> se som is <math>180^\circ</math>]</i> | $\checkmark \quad m_{AU} = -2$<br>$\checkmark \quad m_{AD} = \frac{1}{2}$<br>$\checkmark \quad m_{AU} \times m_{DA} = -1$<br>$\checkmark \quad \hat{A} = 90^\circ$<br>$\checkmark \quad D\hat{Q}U = 90^\circ$<br>$\checkmark \quad R$ | (6)  |
|     |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      |                                                                                                                                                                                                                                       | [20] |

| QUESTION 5 / VRAAG 5 |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        |                                                                                                                                                                       |     |
|----------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----|
|                      |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        |                                                                                                                                                                       |     |
| 5.1.1                | $\sin(-52^\circ) = -\sin 52^\circ$<br>$= \sqrt{1-t^2}$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 | ✓ $-\sin 52^\circ$<br>✓ ✓ answer                                                                                                                                      | (3) |
| 5.1.2                | $\cos(2 \cdot 19^\circ) = \cos 38^\circ$<br>$2 \cos^2 19^\circ - 1 = \cos 38^\circ$<br>$\cos 19^\circ = \sqrt{\frac{\cos 38^\circ + 1}{2}}$<br>$\therefore \cos 19^\circ = \sqrt{\frac{\sqrt{1-t^2} + 1}{2}}$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          | ✓ $\cos(2 \cdot 19^\circ) = \cos 38^\circ$<br>✓ $\cos(2 \cdot 19^\circ) = 2 \cos^2 19^\circ - 1$<br><br>✓ simplification / vereenvoudiging<br><br>✓ answer / antwoord | (4) |
| 5.2                  | $\frac{2 \cos(180^\circ + x) \cdot \sin(180^\circ - x) \cdot \sin 74^\circ}{\sin(x + 360^\circ) \cdot \sin 37^\circ \cdot \sin 53^\circ \cdot \sin(x - 90^\circ)}$ $= \frac{2(-\cos x) \cdot \sin x \cdot \sin 74^\circ}{\sin x \cdot \sin 37^\circ \cdot \cos 37^\circ \cdot (-\cos x)}$ $= \frac{2 \sin 74^\circ}{\frac{1}{2} \sin 74^\circ}$ $= 4$ <p>OR/OF</p> $\frac{2 \cos(180^\circ + x) \cdot \sin(180^\circ - x) \cdot \sin 74^\circ}{\sin(x + 360^\circ) \cdot \sin 37^\circ \cdot \sin 53^\circ \cdot \sin(x - 90^\circ)}$ $= \frac{2(-\cos x) \cdot \sin x \cdot \sin(2 \times 37^\circ)}{\sin x \cdot \sin 37^\circ \cdot \cos 37^\circ \cdot (-\cos x)}$ $= \frac{2 \sin(2 \times 37^\circ)}{\sin 37^\circ \cdot \cos 37^\circ}$ $= \frac{4 \sin 37^\circ \cdot \cos 37^\circ}{\sin 37^\circ \cdot \cos 37^\circ}$ $= 4$ | ✓ $-\cos x$<br>✓ $\sin x$<br>✓ $\sin x$<br>✓ $\cos 37^\circ$<br>✓ $-\cos x$<br>✓ $\frac{1}{2} \sin 74^\circ$<br>✓ answer / antwoord                                   | (7) |

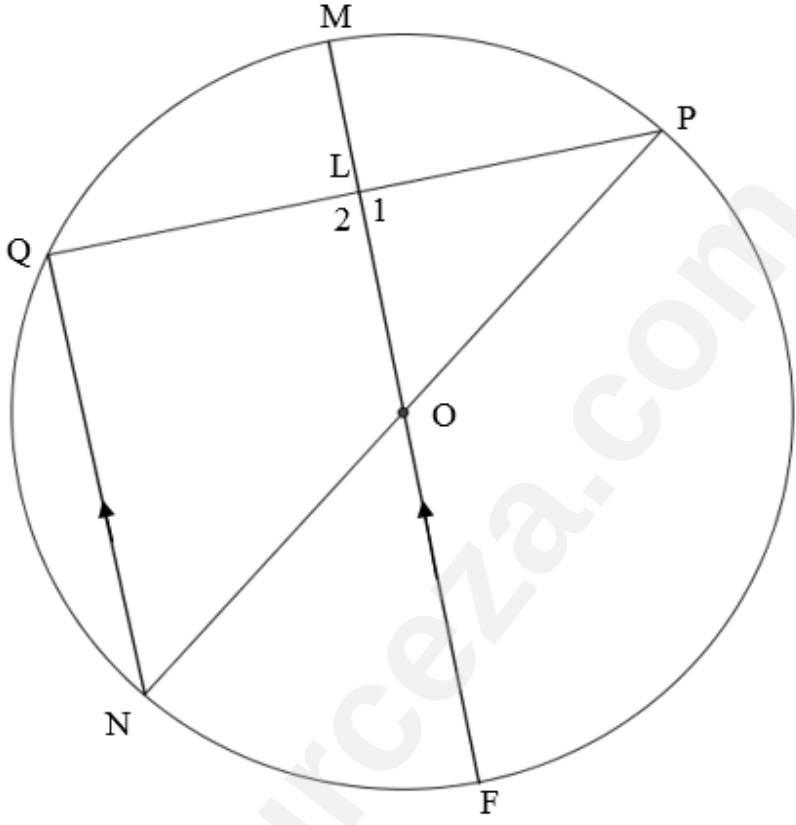
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|-------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------|------|
| 5.3.1 | $1 - \cos 2x = 0$<br>$\cos 2x = 1$<br>$\therefore 2x = 0^\circ + k \cdot 360^\circ$<br>$x = 0^\circ + k \cdot 180^\circ; k \in \mathbb{Z}$                                                                                                                     | $\checkmark 1 - \cos 2x = 0$<br>$\checkmark 2x = 0^\circ + 360^\circ \cdot k$<br>$\checkmark x = 0^\circ + 180^\circ \cdot k;$<br>$\checkmark k \in \mathbb{Z}$ | (4)  |
| 5.3.2 | $\begin{aligned} \text{L.H.S/LK} &= \frac{2\sin x}{2(1 - \cos 2x)} \\ &= \frac{2\sin x}{2 - 2\cos 2x} \\ &= \frac{2\sin x}{2 - 2(1 - 2\sin^2 x)} \\ &= \frac{2\sin x}{2 - 2 + 2\sin^2 x} \\ &= \frac{2\sin x}{2\sin^2 x} \\ &= \frac{1}{\sin x} \end{aligned}$ | $\checkmark 1 - 2\sin^2 x$<br>$\checkmark$ removing brackets<br><i>verwyder hakies</i><br>$\checkmark 2\sin^2 x$                                                | (3)  |
|       |                                                                                                                                                                                                                                                                |                                                                                                                                                                 | [21] |

| QUESTION 6 / VRAAG 6 |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          |                                                                                                                                                                                                                                                                                          |             |
|----------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------|
| 6.1                  | $\sin(x + 60^\circ) = \sin(90^\circ - 2x)$<br>$\therefore x + 60^\circ = 90^\circ - 2x + 360^\circ.k$ or/of $x + 60^\circ = 180^\circ - (90^\circ - 2x) + 360^\circ.k$<br>$3x = 30^\circ + 360^\circ.k$ or/of $x = -30^\circ + 360^\circ.k$<br>$x = 10^\circ + 120^\circ.k$ ; $k \in \mathbb{Z}$<br>$\therefore x = -30^\circ ; 10^\circ ; 130^\circ$<br><br><b>OR/OF</b><br><br>$\cos 2x = \cos(30^\circ - x)$<br>$2x = 30^\circ - x + 360^\circ.k$ or $2x = -(30^\circ - x) + 360^\circ.k$ ; $k \in \mathbb{Z}$<br>$3x = 30^\circ + 360^\circ.k$ or $x = -30^\circ + 360^\circ.k$<br>$\therefore x = -30^\circ ; 10^\circ ; 130^\circ$ | ✓ co-ratio / ko-funksie<br><br>✓ both gen. solns<br><i>beide algemene oplossings</i><br>✓ $-30^\circ$<br>✓ $10^\circ$<br>✓ $130^\circ$<br><br>✓ co-ratio / ko-funksie<br><br>✓ both gen. solns<br><i>beide algemene oplossings</i><br><br>✓ $-30^\circ$<br>✓ $10^\circ$<br>✓ $130^\circ$ | (5)         |
| 6.2                  |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          | g:<br>✓ x-intercept.<br><i>x-afsnit</i><br>✓ y-intercept.<br><i>y-afsnit</i><br>✓ shape / vorm<br><br>f:<br>✓ x-intercept.<br><i>x-afsnit</i><br>✓ y-intercept.<br><i>y-afsnit</i><br>✓ shape / vorm                                                                                     | (6)         |
| 6.3                  | $240^\circ$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              | ✓ answer / antwoord                                                                                                                                                                                                                                                                      | (1)         |
| 6.4                  | $h(x) = \cos(2x - 90^\circ) - 1 = \sin 2x - 1$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | ✓ substitution / vervanging<br>✓ $\sin 2x - 1$                                                                                                                                                                                                                                           | (2)         |
|                      |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          |                                                                                                                                                                                                                                                                                          | <b>[14]</b> |

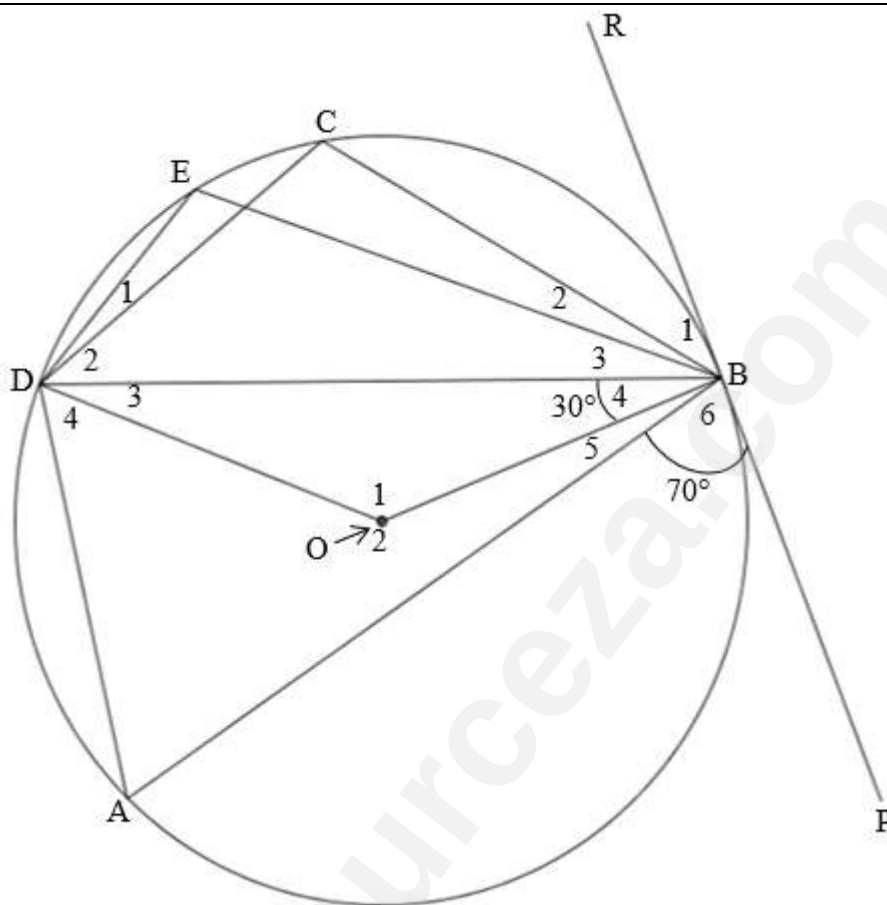
## QUESTION 7 / VRAAG 7



|            |                                                                                                                    |                                                                                                                                                                       |     |
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| 7.1        | $NP^2 = ON^2 + OP^2$ $= (103)^2 + (145)^2$ $\therefore NP = 177,86$                                                | <ul style="list-style-type: none"> <li>✓ using Pyth theorem correctly<br/><i>korrekte gebruik van stelling van Pythagoras</i></li> <li>✓ answer / antwoord</li> </ul> | (2) |
| 7.2        | $PQ^2 = (103)^2 + (103)^2 - 2(103)(103)\cos(120^\circ)$ $PQ = 178,40$                                              | <ul style="list-style-type: none"> <li>✓ subst. into cosine rule<br/><i>verv. in cosinus formule</i></li> <li>✓ answer / antwoord</li> </ul>                          | (2) |
| 7.3        | $\cos \hat{N} = \frac{(177,86)^2 + (177,86)^2 - (178,40)^2}{2(177,86)(177,86)}$ $\therefore \hat{N} = 60,20^\circ$ | <ul style="list-style-type: none"> <li>✓ substitution / <i>vervangings</i></li> <li>✓ <math>\hat{N}</math></li> </ul>                                                 | (2) |
| <b>[6]</b> |                                                                                                                    |                                                                                                                                                                       |     |

| QUESTION 8 / VRAAG 8 |                                                                                                                                                                                                                                                                                                                                                 |                                                                                                                           |     |
|----------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------|-----|
| 8.1                  | Bisects the chord / <i>Halveer die koord</i>                                                                                                                                                                                                                                                                                                    | ✓ answer / <i>antwoord</i>                                                                                                | (1) |
| 8.2                  |                                                                                                                                                                                                                                                              |                                                                                                                           |     |
| 8.2.1                | $\hat{Q} = 90^\circ$ [ $\angle$ in semi circle. ] / [ $\angle$ in halwe sirkel ]<br>$\hat{L}_1 = \hat{Q} = 90^\circ$ [corresp. $\angle^s$ , $QN \parallel LO$ ]<br><i>[ooreenk. <math>\angle^e</math>, <math>QN \parallel LO</math>]</i><br>$QL = LP$ [line from centre perp. to chord]<br><i>[lynstuk vanaf middelpnt is loodreg op koord]</i> | ✓ S ✓ R<br>✓ S/R<br><br>✓ R                                                                                               | (4) |
| 8.2.2                | $MF = 8ML$                                                                                                                                                                                                                                                                                                                                      | ✓                                                                                                                         | (1) |
| 8.2.3                | $OP^2 = OL^2 + LP^2$<br>$(4ML)^2 = (3ML)^2 + 7^2$<br>$16ML^2 = 9ML^2 + 49$<br>$7ML^2 = 49$<br>$\therefore ML = \sqrt{7}$                                                                                                                                                                                                                        | ✓ using Pyth correctly<br><i>korrekte gebruik van Pythagoras</i><br><br>✓ simplification / <i>vereenvoudiging</i><br>✓ ML | (3) |
|                      |                                                                                                                                                                                                                                                                                                                                                 |                                                                                                                           | [9] |

**QUESTION 9 / VRAAG 9**

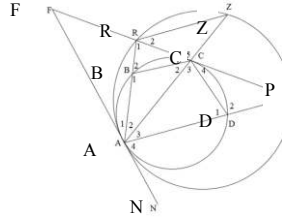


|     |                                                                                                                                                                                                                                         |                 |            |
|-----|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------|------------|
| 9.1 | $\hat{D}_3 = 30^\circ$ [ $\angle$ s opp equal sides] / [ $\angle^e$ teenoor gelyke sye]<br>$\therefore \hat{O}_1 = 120^\circ$ [sum of $\angle$ s of a $\Delta$ .] / [ <i>som v/d <math>\angle^e</math> van 'n <math>\Delta</math></i> ] | ✓ S ✓R<br>✓ S/R | (3)        |
| 9.2 | $\hat{A} = 60^\circ$ [ $\angle$ at centre = 2 $\angle$ at circumf.] /<br><i>[middelpunts <math>\angle</math> = 2 <math>\times</math> omtrekshoek]</i>                                                                                   | ✓ S ✓R          | (2)        |
| 9.3 | $\hat{C} = 120^\circ$ [opp. $\angle$ s of cyclic quad.] / [ <i>teenoorst. <math>\angle^e</math> van k.v</i> ]                                                                                                                           | ✓ S ✓R          | (2)        |
| 9.4 | $\hat{ADB} = 70^\circ$ [tan chord theorem.] / [ <i>raaklyn koord stelling</i> ]                                                                                                                                                         | ✓ S ✓R          | (2)        |
|     |                                                                                                                                                                                                                                         |                 | <b>[9]</b> |

| QUESTION 10 / VRAAG 10 |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  |                                  |     |
|------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------|-----|
| 10.1                   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | ✓ constr.<br>konstr.             |     |
|                        | $\hat{U}_2 = 90^\circ - \hat{U}_1$ [tan $\perp$ radius.] / [raaklyn $\perp$ radius]<br>$\hat{Z} = 90^\circ$ [ $\angle$ in semi circle] / [ $\angle$ in halwe sirkel]<br>$\hat{S} = 180^\circ - (90^\circ - \hat{U}_1) - 90^\circ$ [sum of $\angle$ s of a $\Delta$ ]<br>$\therefore \hat{S} = \hat{U}_1$ [som van die $\angle$ e van 'n $\Delta$ ]<br>$\hat{S} = \hat{Y}$ [ $\angle$ s in same segment] / [ $\angle$ e in dieselfde segment]<br>$\therefore \hat{U}_1 = \hat{Y}$ | ✓ S/R<br>✓ S/R<br>✓ S/R<br>✓ S/R | (5) |



## QUESTION 11 / VRAAG 11



|      |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 |                                                                                                                                                                       |      |
|------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------|------|
| 11.1 | $\hat{A}_1 = \hat{C}_2$ [tan chord theo.] / [raaklyn koord stelling]<br>$= \hat{Z}$ [tan chord theo.] / [raaklyn koord stelling]<br>$\therefore \hat{C}_2 = \hat{Z}$ [both = x] / [beide = x]<br>$\therefore BC \parallel RZ$ [corresp. $\angle$ s =] / [ooreenk. $\angle$ e =]                                                                                                                                                                                                                                                                                                                                                                 | $\checkmark$ S $\checkmark$ R<br>$\checkmark$ S/R<br>$\checkmark$ R                                                                                                   | (4)  |
| 11.2 | $\hat{Z} = \hat{P}$ [ $\angle$ s in same segment] / [ $\angle$ e in dieselfde segment]<br>$= \hat{C}_2$ [corresp. $\angle$ s ; $BC \parallel RZ$ ] / [ooreenk. $\angle$ e ; $BC \parallel RZ$ ]<br>$\therefore BC$ is a tangent to circle ACP [conv. of tan chord theorem]<br><i>BC is 'n raaklyn aan sirkel ACP [ omgekeerde van raaklyn koord stelling]</i>                                                                                                                                                                                                                                                                                   | $\checkmark$ S/R<br>$\checkmark$ S<br><br>$\checkmark$ R                                                                                                              | (3)  |
| 11.3 | $\hat{B}_1 = \hat{D}_2$ [ext. $\angle$ of a cyclic quad.]<br><i>[buite <math>\angle</math> van koordevierhoek]</i><br>$\hat{R} = \hat{B}_1$ [corresp. $\angle$ s , $BC \parallel RZ$ ]<br><i>[ooreenk. <math>\angle</math>e , <math>BC \parallel RZ</math>]</i><br>$\therefore \hat{R} = \hat{D}_2$<br>$\hat{Z} = \hat{P}$ [ $\angle$ s in same segment]<br><i>[<math>\angle</math>e in dieselfde segment]</i><br>$\hat{A}_2 = \hat{C}_4$ [ $3^{rd}$ $\angle$ ] / [ $3^{de}$ $\angle$ ]<br>$\therefore \triangle RZA \parallel \triangle DPC$ [equiangular or $\angle\angle\angle$ ]<br><i>[gelykhoekig of <math>\angle\angle\angle</math>]</i> | $\checkmark$ S $\checkmark$ R<br>$\checkmark$ S/R<br>$\checkmark$ S/R<br>$\checkmark$ R                                                                               | (5)  |
| 11.4 | $\frac{ZA}{PC} = \frac{RA}{DC}$ [similar $\Delta$ s] / [gelykvormige $\Delta$ e]<br>$\therefore RA = \frac{ZA \times DC}{PC} \dots (1)$<br>$\frac{AR}{AB} = \frac{AZ}{AC}$ [line $\parallel$ to one side of a $\Delta$ ]<br><i>[lynstuk <math>\parallel</math> aan een sy van 'n <math>\Delta</math>]</i><br>$\therefore AR = \frac{AZ \times AB}{AC} \dots (2)$<br>$\frac{ZA \times DC}{PC} = \frac{AZ \times AB}{AC}$<br>$\therefore \frac{DC}{PC} \times \frac{AC}{AB} = 1$                                                                                                                                                                  | $\checkmark$ S/R<br>$\checkmark$ $RA = \frac{ZA \times DC}{PC}$<br>$\checkmark$ S/R<br><br>$\checkmark$ $RA = \frac{AZ \times AB}{AC}$<br>$\checkmark$ simplification | (5)  |
|      |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 |                                                                                                                                                                       | [17] |
|      |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 | TOTAL/TOTAAL:                                                                                                                                                         | 150  |